

CS403/SE307/CS355 – Computation and Complexity
Department of Computer Science
National University of Ireland, Maynooth

T Naughton, NUIM
<http://www.cs.may.ie/~tนาughton/teaching/se307>

Template for undecidability proofs using a mapping reduction

Proof. We will use a mapping reduction to prove the reduction _____.
Assume that _____ is decidable. The function f that maps instances of _____
to instances of _____ is performed by TM F given by the following pseudocode.

$F =$ “On input $\langle \text{_____} \rangle$:

1. Construct the following M' given by the following pseudocode.

$M' =$ “ _____

_____”

2. Output $\langle \text{_____} \rangle$ ”

Now, $\langle \text{_____} \rangle$ is an element of _____ iff $\langle \text{_____} \rangle$ is an element
of _____. So using f and the assumption that _____ is decidable, we can
decide _____. A contradiction. Therefore, _____ is undecidable. (This
also proves that the complement of _____ is undecidable, because the complement
of any undecidable language is itself undecidable.)